The Ludii Game Description Language is Universal

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Abstract
There are several different game description languages (GDLs), each intended to allow wide ranges of arbitrary games (i.e., general games) to be described in a single higher-level language than general-purpose programming languages. Games described in such formats can subsequently be presented as challenges for automated general game playing agents, which are expected to be capable of playing any arbitrary game described in such a language without prior knowledge about the games to be played. The language used by the Ludii general game system was previously shown to be capable of representing equivalent games for any arbitrary, finite, deterministic, fully observable extensive-form game. In this paper, we prove its universality by extending this to include finite non-deterministic and imperfect-information games.

1 Introduction
General Game Playing (GGP) is a subfield of Artificial Intelligence (AI) research, in which the challenge is to develop agents that can successfully play arbitrary games without human intervention or prior knowledge of exactly which games are to be played [Pitrat, 1968]. Implementing such an agent in practice typically requires the use of a Game Description Language (GDL); a standardised format such that the rules of any game can be provided to an agent without having to implement it directly in a general-purpose programming language.

The GDL that popularised GGP research [Genesereth et al., 2005; Love et al., 2008] originated primarily from Stanford; we refer to it as S-GDL in this paper. Other systems with GDLs include Regular Boardgames (RBG) [Kowalski et al., 2019] and Ludii [Browne et al., 2020b; Piette et al., 2020] for general games, as well as GVGAI [Schaul, 2014; Perez-Liebana et al., 2019] for video games. Aside from facilitating GGP research, the use of domain-specific languages has also been proposed for the ease with which they enable the implementation of custom, targeted testbeds [Samvelyan et al., 2021].

S-GDL is a relatively low-level logic-based GDL. After the introduction of an extension to support randomness and imperfect information [Thielscher, 2010], it was proven that S-GDL is universal [Thielscher, 2011]: any arbitrary finite extensive-form [Rasmussen, 2007] game can be faithfully represented in a legal S-GDL description. For the GDL of RBG, this was only proven for the subset of fully-observable, deterministic games [Kowalski et al., 2019]. Similarly, Ludii’s GDL (L-GDL) was previously only proven to be capable of representing any finite, deterministic, perfect-information, alternating-move game, although it did already include basic support for stochasticity and hidden information (without a proof of universality) [Piette et al., 2020].

For S-GDL, the proof of its universality [Thielscher, 2011] essentially consists of encoding the entire game tree of any arbitrary finite extensive-form game in logic statements. L-GDL is a comparatively higher-level language that primarily consists of many keywords that game designers and players can readily understand as common game terms, such as board, piece, slide, hop, and so on. By design, it is intended to be easier to read, understand and use for game designers [Browne, 2016], with less of a focus on including the low-level language elements that would enable the exhaustive enumeration of all states of an extensive-form game tree. It has a relatively tightly-enforced structure, with many enforced restrictions due to strong typing. In comparison to the lower-level S-GDL with a relatively flat structure that makes it straightforward to exhaustively enumerate a complete game tree, this makes it non-trivial to prove a similar level of generality for L-GDL. Nevertheless, in this paper we are able to prove the universality of L-GDL by demonstrating that it can represent the same class of games as proven by Thielscher [2011] for S-GDL, including games with randomness and hidden information. This provides a theoretical argument that L-GDL is a suitable, sufficiently general and powerful description language for problems for AI research.

2 Background
In this section, we provide background information on the standard, universal formalism of extensive-form games, as well as L-GDL.
2.1 Extensive-Form Games

Extensive-form games [Rasmusen, 2007] are a standard, general formalisation of games in the broad, mathematical sense of the word (i.e., including many decision-making problems that would not generally be viewed by most humans as “fun” games). The formal definition is as follows:

**Definition 1.** An extensive-form game $G$ is specified by a tuple $G = \langle \mathcal{P}, \mathcal{T}, \mathcal{U}, \iota, D, I \rangle$, where:

- $\mathcal{P} = \{1, 2, \ldots, k, \eta\}$ is a finite set of $k \geq 1$ players, and a “nature” player $\eta$ to model stochastic events.
- $\mathcal{T}$ is a tree, where every node represents a single game state $s \in \mathcal{S}$. The full set of states $\mathcal{S} = \mathcal{S}_{inn} \cup \mathcal{S}_{ter}$ may be partitioned into a subset of non-terminal states (inner nodes) $\mathcal{S}_{inn}$ and a subset of terminal states (leaf nodes) $\mathcal{S}_{ter}$, such that $\mathcal{S}_{inn} \cap \mathcal{S}_{ter} = \emptyset$.
- $\mathcal{U} : \mathcal{S}_{ter} \rightarrow \mathbb{R}^k$ is a payoffs function, such that $\mathcal{U}(s)$ denotes a vector of $k$ real-valued payoffs (for the $k$ players) for any terminal game state $s \in \mathcal{S}_{ter}$.
- $\iota : \mathcal{S}_{inn} \rightarrow \mathcal{P}$ is a function such that, for any non-terminal game state $s \in \mathcal{S}_{inn}$, $\iota(s)$ gives the player to play in that state.
- $D : \{(s, s') \mid \iota(s) = \eta, s \in \mathcal{S}_{inn}, s' \in \mathcal{S}\} \rightarrow \mathcal{R}$ gives, for any non-terminal state $s$ controlled by the nature player $\eta$, a probability $0 \leq D(s, s') \leq 1$ that the nature player “selects” $s'$ as the successor. Note that this must yield proper probability distributions over successors, i.e. $\forall s \in \mathcal{S} \mid \iota(s) = \eta, s \in \mathcal{S}_{inn} : \sum_{s' \in \mathcal{S}} D(s, s') = 1$.
- $I : \{(p, s) \mid p \in \mathcal{P} \setminus \{\eta\}, s \in \mathcal{S} \} \rightarrow \mathcal{P}(\mathcal{S})$, where $\mathcal{P}(\mathcal{S})$ denotes the powerset of $\mathcal{S}$, gives the information set $I(p, s)$ of player $p$ for state $s$ (i.e., the set of states that are indistinguishable from each other from the perspective of player $p$ when the true state is $s$).

In this paper, we focus on finite extensive-form games $G$, where $\mathcal{T}$ is of a finite size. Furthermore, we focus on alternating-move games, since the function $\iota$ only gives a single player to move per game state $s$. In theory, this is without loss of generality, since any simultaneous-move game can be equivalently modelled as an alternating-move game in which the effects of moves are delayed until every active player in a turn has selected their move, and moves within the same turn are hidden information for all other players [Watson, 2013]. In practice, Ludii does contain additional support for modelling simultaneous-move games, but for our theoretical analysis we do not need this.

2.2 L-GDL

The basic structure of an L-GDL game description is depicted in Figure 1. It is defined by a grammar, automatically derived from Ludii’s source code [Browne, 2016], which specifies which keywords (also referred to as ludemes) and types of data (strings, integers, real numbers, and so on) can or cannot be used depending on the context. As shown by Figure 1, a game description file is expected to describe exactly one game, which has three top-level entries:

1. **players**: describes basic data about the players (e.g., how many players the game is played by).
2. **equipment**: describes aspects such as any board(s) or graph(s) the game is played on, types of pieces or dice used in the game, and so on.
3. **rules**: describes rules used to (i) **start** the game (generate initial game state, e.g. by placing initial pieces on a board), (ii) **play** the game (generate lists of legal moves), and (iii) **end** the game (evaluate whether a state is terminal and determine the outcomes for the players). Some of these aspects must be specified (such as the play rules), whereas others may be omitted if unnecessary (e.g., start rules are unnecessary in games that start with an empty board) or if they have a suitable default value (e.g., Ludii assumes a default number of players of 2 if left unspecified).

Piette et al. [2020] provide more detailed information on the Ludii system, and Browne et al. [2020a] provide a complete, detailed language reference for L-GDL. A full example description for the game of Tic-Tac-Toe is presented in Figure 2.

3 From Extensive-Form Games to L-GDL

Given any arbitrary finite, extensive-form game $G = \langle \mathcal{P}, \mathcal{T}, \mathcal{U}, \iota, D, I \rangle$ as defined in Definition 1, we describe how a corresponding Ludii game $G^L$ can be modelled in L-GDL. In Section 4, we formally state and prove the theorem that $G$ and $G^L$ form equivalent game trees with one-to-one correspondences between the set of all possible trajectories in $G$ and the set of all possible trajectories in $G^L$. For simplicity, and without loss of generality, we make several assumptions about $G$:

**Assumption 1.** $G$ has a single, unique initial game state so as root node of its game tree.

This assumption is without loss of generality because a game with multiple distinct possibilities for the initial game state can be equivalently modelled as a game with a single chance node as root, with appropriate probabilities assigned for all the intended “real” initial game states.

**Assumption 2.** If the root node of $G$ is not a chance node, the player labelled as 1 will be the first player to make a move.

This assumption is without loss of generality because there is otherwise no particular meaning to the labels that are assigned to players.

The following subsections describe how to fill in the basic template L-GDL description from Figure 1 to construct such a Ludii game $G^L$. The intuition behind our approach is similar to that of the proof by Piette et al. [2020] (which was restricted to deterministic, perfect-information settings) in the sense that we explicitly enumerate the entire game tree of $G$ as a graph that the players play on by moving stones along a path from the root to any leaf. The most significant change is that, to support imperfect-information settings, we now use multiple “copies” of such a graph, with sets of possibly more than one stone per player moving down each player’s respective tree to track the information sets (rather than individual states) that players navigate between.
Thirdly, for every state $s_i \in \mathcal{S}$ and every player $1 \leq p \leq k$, we define a region in the equipment that contains all the indices of the vertices corresponding to states that are in the information set of $p$ when the true state is $s_i$. More formally, for all $0 \leq i < |\mathcal{S}|$ and all $1 \leq p \leq k$, we define a region named "$\text{InformationSet}_{i,p}$" containing all the indices $p \times |\mathcal{S}| + j$ for all $j \in \{j \mid s_j \in \mathcal{I}(s_i, p)\}$. Such a region can be defined in a game description using (regions "$\text{InformationSet}_{i,p}$" {...}). Whenever we know that the true state is $s_i$, this region allows us to easily access all the vertices corresponding to the complete information set for any given player $p$.

Fourthly, for every player $1 \leq p \leq k$, we define a region in the equipment named "$\text{Subgraph}_{p}$" that contains all the indices of the vertices in that player’s respective subgraph, i.e. all indices in $\{j \mid p \times |\mathcal{S}| \leq j < (p + 1) \times |\mathcal{S}|\}$. Such a region can be defined in a game description using (regions "$\text{Subgraph}_{p}$" {...}). We similarly define a region "$\text{Subgraph}_{\emptyset}$" for the first subgraph.

### 3.3 Defining the Start Rules

Due to Assumption 1, we know that every player’s information set for the initial game state contains only $s_0$: $\forall_p \mathcal{I}(s_0, p) = \{s_0\}$. Hence, we start the game by placing a marker for each player (including a neutral marker for the nature player) on the vertex that represents the initial game state in each player’s respective subgraph in the board. For any player $p$, the index of this vertex is given by $p \times |\mathcal{S}|$, assuming $p = 0$ for the nature player. Presence or absence of markers on any site in a subgraph corresponding to a player $p$ must be hidden from all other players $p' \neq p$, to avoid leaking information that those other players should not have access to. Start rules that accomplish this setup for the initial game state are provided in Figure 3.

### 3.4 Defining the Play Rules

The play rules in Ludii define how to generate a list of legal moves for any given current game state $s_i$. In our $\mathcal{G}^L$ model, where we aim to replicate the structure of the game tree of the extensive-form game $\mathcal{G}$, we may distinguish two primary cases:

1. If $s_i$ is a chance node, i.e. $\mathcal{I}(s_i) = \eta$, in Ludii a regular player will be in control because Ludii does not explicitly include a nature player. Hence, we should generate only a single legal move such that the player is forced to traverse the branch that the chance player would have picked in $\mathcal{G}$. This can be accomplished by using the (random {...} {...}) ludeme, where the first array contains a sequence of $n$ weights, and the second array contains a sequence of $n$ move-generating ludemes, for a chance node with $n$ possible branches. For example, (random \{ $p$, $q$, $r$ \} \{ A B C \}) randomly selects one of the ludemes $A$, $B$, or $C$ to generate the list of legal moves, with probabilities $\frac{p}{p+q+r}$, $\frac{q}{p+q+r}$, or $\frac{r}{p+q+r}$, respectively. The appropriate weights to use can be derived from the nonzero probabilities $\mathcal{D}(s, s')$ as specified in $\mathcal{G}$.
... (start {
  (place "Marker0" 0)
  (place "Marker1" <1 × |S|>)
...
  (place "Markerk" <k × |S|>)
  (set Hidden
    (sites "Subgraph_0") to: All)
  (set Hidden
    (sites "Subgraph_1") to: (player 2))
...
  (set Hidden
    (sites "Subgraph_1") to: (player k))
  (set Hidden
    (sites "Subgraph_2") to: (player 1))
  (set Hidden
    (sites "Subgraph_2") to: (player 3))
...
  (set Hidden
    (sites "Subgraph_2") to: (player k))
...
  (set Hidden
    (sites "Subgraph_k") to: (player k - 1))
})
...

Figure 3: Start rules for a Ludii game \(G^L\), modelling an equivalent extensive-form game \(G\), with \(k\) players. The expressions to compute vertex indices in angled brackets are used for generality, but would be replaced by the concrete result of the expression in any single concrete game description.

2. If \(s_i\) is not a chance node, i.e. \(\iota(s_i) \neq \eta\), the mover \(\iota(s_i)\) should have one move corresponding to every branch from \(s_i\) in the game tree of the extensive-form game \(G\). This can be implemented using an (or \{ ... \}) ludeme that wraps around other ludemes, each of which generates one of the legal moves.

Without any knowledge of any general rules that may determine how legal moves are computed from a game state \(s_i\) in the extensive-form game \(G\), it is necessary to explicitly enumerate all game states and define the play rules separately per state. One way to accomplish this is by using a chain of (if \(C \land A \land B\)) ludemes, where:

- \(C\) is a condition of the form (= (where "Marker" Neutral) i): this checks whether the Marker \(0\) piece is located on vertex \(i\), and can hence be used to determine whether or not the current game state is \(s_i\).
- \(A\) is a ludeme that generates the moves in the case that the condition of \(C\) is satisfied by the current game state (i.e., if the current game state is \(s_i\)).
- \(B\) is a ludeme that generates the moves if the current game state does not satisfy the condition of \(C\); this can again be a ludeme of the same (if \(C \land A \land B\)) form.

Suppose that there is some branch in the extensive-form game tree of \(G\) that leads from a state \(s_i\) to a state \(s_j\). In the corresponding Ludii game \(G^L\), we require a corresponding move that has the following effects on the game state:

1. It should move the Marker \(0\) piece, which should currently be located on the vertex with index \(i\), to the vertex with index \(j\). This enables us to continue tracking the true game state.
2. For every player \(1 \leq p \leq k\), any Marker \(k\) pieces currently on the board should be removed, and new Marker \(k\) pieces should be placed on all vertices in the InformationSet \(-j\) \(p\) region. This enables us to let every player know which information set it transitioned into.
3. By default, Ludii reveals information about positions that become empty. Because the above effects remove some pieces from positions that should still remain hidden from many players, vertices should be appropriately set to hidden again as they were originally set in the start rules.
4. By default, Ludii updates the index of which player is designated the mover after every move, by incrementing it or resetting it to 1 after player \(k\) made a move. If this results in a different player to move than the player \(\iota(s_j)\) that should become the mover in \(s_j\), we need to include an extra effect in the move that correctly sets the player to move. Note that, if \(\iota(s_j) = \eta\) in \(G\), it does not matter which player is set to be the mover in Ludii, since we only generate one legal move anyway that whichever player is the mover will be forced to pick.

Suppose that such a state \(s_i\) has \(n\) legal moves. A straightforward way to present \(n\) different options to the player \(\iota(s_i)\) is to allow them to select one out of any of \(v\) vertices \(v < n\), and for each of those “select” moves specify appropriate consequences. These consequences should correspond to the \(n\)th branch from \(s_i\) in the game tree of \(G\), but otherwise do not necessarily have any particular relationship with the specific vertex \(v\); selecting vertices is simply a mechanism through which the player can distinguish between \(n\) different moves. Figure 4 depicts the specification of a move rule for a single transition from \(s_i\) to \(s_j\).

3.5 Defining the End Rules

For each of the terminal game states \(s_t \in \mathcal{S}_{ter}\) in \(G\), we can define a separate end rule in \(G^L\) that checks whether that specific state has been reached by tracking the position of the Marker \(0\) piece, and assigns a vector of payoffs to the \(k\) players as given by \(U(s_t)\) using the payoffs ludeme. Figure 5 provides an example of such end rules for an example game for \(k = 3\) players with two terminal game states.

4 Proof of Equivalence

Based on the strategy for constructing a Ludii game \(G^L\) for any extensive-form game \(G\) as described above, we present Theorem 1, which may intuitively be understood as stating that it is possible to model any arbitrary finite extensive-form game in L-GDL.

Theorem 1. Under Assumptions 1 and 2, for any arbitrary extensive-form game \(G\), a corresponding Ludii game \(G^L\) constructed as described in Subsections 3.1–3.5, is equivalent to \(G\) in the sense that the following criteria are satisfied:
Figure 4: Ludeme generating a move corresponding to the \( n \)^{th} branch from a state \( s_i \), leading to a state \( s_j \), in the game tree of an extensive-form game \( G \) with \( k \) players. The player that should be the mover in the next state \( s_j \) is denoted by \( \iota(s_j) \)—except we replace it by any arbitrary integer in \([1, k]\) if \( \iota(s_j) = \eta \).

\[
\begin{align*}
\text{(move Select (from } n) \\
\text{(then (and { (fromTo (from } i) (to } j)) (remove (sites Occupied by: P1)) (remove (sites Occupied by: P2)) (remove (sites Occupied by: Pk)) (add (piece 1) (to (sites "InformationSet_1"))) (add (piece 2) (to (sites "InformationSet_2"))) (add (piece k) (to (sites "InformationSet_k"))) (set Hidden (sites "Subgraph_0") to: All) (set Hidden (sites "Subgraph_k") to: (player k)) (set Hidden (sites "Subgraph_1") to: (player k)) (set Hidden (sites "Subgraph_2") to: (player 1)) (set Hidden (sites "Subgraph_2") to: (player 3)) (set Hidden (sites "Subgraph_2") to: (player k)) (set Hidden (sites "Subgraph_k") to: (player k-1)) (set NextPlayer (player \iota(s_j))))})
\end{align*}
\]

end \{
\begin{align*}
\text{(if (= (where "Marker" Neutral) 88)) (payoffs { (payoff P1 -1) (payoff P2 0.5) (payoff P3 1)})
\text{(if (= (where "Marker" Neutral) 2077)) (payoffs { (payoff P1 10) (payoff P2 12) (payoff P3 2020)})
\text{))}}
\end{align*}
\]

Figure 5: Example end rules for an example game with \( k = 3 \) players, where states \( s_{88} \) and \( s_{2077} \) are terminal states, with payoff vectors of \([-1, 0.5, 1] \) and \([10, 12, 2020]\), respectively.

1. The game description of \( G^L \) is a valid game description according to the specification of L-GDL.
2. There exists a one-to-one correspondence between trajectories from the root node to any possible leaf node in the game tree of \( G \), and trajectories of play that are possible from the initial game state in \( G^L \). More concretely, this means that:

   (a) For every node \( s \) that is reachable from the root node \( s_0 \), including \( s_0 \) itself, there exists an equivalent game state in \( G^L \) that is also reachable in the same number of transitions from the initial game state of \( G^L \).

   (b) For every node \( s \) in the game tree of \( G^L \) where \( \iota(s) \neq \eta \) (i.e., any node that is not a chance node), the equivalent state in \( G^L \) also has \( \iota(s) \) as the player to move.

   (c) For every node \( s \) in the game tree of \( G^L \) where \( \iota(s) \neq \eta \), if there are \( n \) branches to \( n \) successors, there are also \( n \) legal moves in the equivalent state in \( G^L \).

   (d) For any chance node \( s \) that is reachable from the root node \( s_0 \) of the game tree of \( G \), for every possible \( s' \) that has a probability \( D(s, s') > 0 \) of being the successor of \( s \), there is also a probability \( \bar{D}(s, s') \) that a transition to the equivalent state of \( s' \) in \( G^L \) is the only legal transition in any arbitrary trajectory that reaches the equivalent of \( s \) in \( G^L \).

   (e) For any terminal node \( s \in S_{ter} \) in the game tree of \( G \), the equivalent state in \( G^L \) is also terminal, and assigns the same vector of payoffs \( U(s) \).

3. Any player \( 1 \leq p \leq k \) playing the Ludii game \( G^L \) cannot distinguish between any pair of states that are the equivalents of two distinct nodes \( s, s' \) if and only if they share the same information set \( I(s, p) = I(s', p) \).

   These criteria are similar to those used for the proof of universality for S-GDL [Thielscher, 2011].
Proof: By construction, the game description as detailed in subsections 3.1 to 3.5 is a valid L-GDL description. As of the public v1.1.17 release of Ludii—which first introduced the (random ...) and (payoffs ...) ludemes—all of the ludemes used are supported. This satisfies criterion 1.

The start rules of \( G^L \) (see Figure 3) ensure that, in the initial game state, a piece of type Marker0 is placed on vertex 0, and not on any other position. All moves that can possibly be generated are of the form depicted in Figure 4, which can only affect the positions of Marker0 pieces through its \((\text{fromTo} \ (\text{from i}) \ (\text{to j}))\) rule, which makes whichever piece is at vertex \( i \) to vertex \( j \). This means that the number of Marker0 pieces cannot change; there must always be one, and only its position can change due to \((\text{fromTo} \ (\text{from i}) \ (\text{to j}))\) rules. For any particular value of \( i \), such a rule is only used in situations that satisfy the \( (= \ (\text{where } \text{"Marker" Neutral} \ 1)) \) condition, i.e. only if vertex \( i \) currently contains the sole Marker0 piece. For any pair of values \( i \) and \( j \), if there is a branch from \( s_i \) to \( s_j \) in the game tree of \( G \), it is also possible for there to be a legal move that moves the Marker0 piece from vertex \( i \) to vertex \( j \) in \( G^L \); such a move is either legal for sure if \( s_i \) is not a chance node, or legal with probability \( D(s_i, s_j) \) if \( s_i \) is a chance node. This satisfies criterion 2a; the equivalent state of a node \( s_i \) can always be identified as the one that has the Marker0 piece on vertex \( i \).

The move rules as described in Figure 4 have, by construction, been set up to ensure that the next player to move is always a marker on every vertex that represents any of the “its own” subgraph. This means that, for any pair of nodes that is in the same information set for a player in the game tree of \( G \), the pair of equivalent game states in \( G^L \) are also indistinguishable from each other from that player’s perspective (due to the arrangement of markers on vertices visible to that player being identical). Note that the move rules as described in Figure 4 were deliberately set up such that players always select vertex \( n \) to pick the \( n^{th} \) move in a list of legal moves, irrespective of which vertices are subsequently affected by that move. It might have been more intuitive to directly select the vertex corresponding to the node in the extensive-form game tree to transition into, but this could reveal additional information that the player should not have access to. With this, criterion 3 is also satisfied and the proof is complete. □

5 Conclusion

Ludii’s game description language (L-GDL) has primarily been designed to be easy to use for game designers, with a focus on facilitating the design of board games and similar abstract games. In practice, its count of over 1,000 distinct game descriptions (which far exceeds the game counts in official repositories of many other systems with GDLs, such as S-GDL [Genesereth et al., 2005; Love et al., 2008], RBG [Kowalski et al., 2019], and GV-GAI [Perez-Liebana et al., 2019]) has already demonstrated its flexibility and generality. In this paper, we have also proven its generality from a theoretical angle, demonstrating that it is possible to write an equivalent game in L-GDL for any arbitrary finite extensive-form game [Rasmusen, 2007]. This provides a significant extension of an earlier proof [Piette et al., 2020] by including stochastic and imperfect-information games, and means that the expressiveness of L-GDL matches that of S-GDL [Thielser, 2011].

This result suggests that we can opt to use Ludii over S-GDL in GGP research for some of its other advantages, such as computational efficiency [Piette et al., 2020] and ease of use, without a loss in expressiveness. While the somewhat convoluted way of defining games used for the theoretical proof is unlikely to be an efficient way of implementing many “real” games in practice, it may be a fruitful starting point for designing synthetic game trees for targeted research into the relations between certain game tree characteristics and the effectiveness of different algorithms [Ramanujan et al., 2010; Ramanujan et al., 2011] within the same framework and API (Ludii) that also supports many real games.

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